$\qquad$ Name: $\qquad$
5.2.1 Do you need a base to have rhythm?

Logarithms

\#37 Leoma has hooked up two function machines as shown in the diagram at right.
a. When Leoma puts 4 into the first machine, 81 comes out. Then the 81 goes into the second machine. What comes out?
b. Next Leoma puts a 2 into the first machine. What number comes out of this machine and goes into the second machine? What then comes out of the second machine?
c. If $x$ goes into the first machine, what comes out of the second machine?

d. How are functions that are inside the function machines related?

You may recall that a logarithm (called a "log" for short) represents the power to which a fixed number (a base) must be raised to produce a given number. For example, $\log _{2}(16)=4$ because $2^{4}=16$. The common logarithm is the logarithm base 10. It is expressed as $\log _{10}(x)$, but more often as $\log (x)$.
\#38 Without a calculator, evaluate each of the following logarithmic expressions. Look for and record any patterns or interesting results.

| a. $\log _{3}(9)$ | b. $\log \sqrt{10}$ | c. $\log _{4}\left(\frac{1}{16}\right)$ | d. $\log (1)$ |
| :--- | :--- | :--- | :--- |
| e. $\log _{7}\left(7^{5}\right)$ | f. $2_{2}^{\log _{2}(16)}$ | g. $\log _{0.2}(5)$ | h. $10^{\log (n)}$ |
| i. $\log _{4}(\sqrt{2})^{3}$ | j. $4^{\log _{2}(9)}$ | k. $\log _{\sqrt{b}}(b)^{3 / 5}$ | I. $4^{\log _{2}(x)}$ |
|  |  |  |  |

\#39 Another useful logarithm is the natural logarithm, or the logarithm base e. It is expressed as $\log _{e}(x)$, but more often as $\ln (x)$. When speaking, the two letters are stated separately as "el en $x$ ". Without a calculator, evaluate each of the following expressions involving the natural logarithm.

| a. $\ln (1)$ | b. $\ln (e)$ | c. $\ln \sqrt{e}$ | d. $e^{\ln (x)}$ |
| :--- | :--- | :--- | :--- |

40. Can a logarithm have any base? Can you take the logarithm of any number? With your team, investigate the possible values of $n, m$, and $b$ in the equation below. Record your conclusions and be prepared to share your findings with the class.

$$
\log _{b}(n)=m
$$

Solve each of the following equations.

$$
\begin{array}{l|l}
\text { a. } \ln \left(\frac{3}{2} x+9\right)=1 & \text { b. } \log (-3)=x
\end{array}
$$

