$\qquad$
5.2.2 What is a logarithm?

Defining the Inverse of an Exponential Function

\#63 Another Ancient Puzzle
Fill in the table with your teammates

| $x$ | 8 | 32 | $\frac{1}{2}$ | 1 | 16 | 4 | 3 | 64 | 2 | 0 | 0.25 | -1 | $\sqrt{2}$ | 0.2 | $\frac{1}{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $g(x)$ | 3 |  | -1 |  |  |  |  | 6 |  |  |  |  |  |  |  |

a. Describe an equation that relates $x$ and $g(x)$.
c. Why is it difficult to think of an output for the input of 0 or -1 ?
b. Look back at the Ancient Puzzle in problem \#54. If you have not already done so, use the idea of the Ancient Puzzle to write an equation for $g(x)$.
d. What is the output for $x=25$, to the nearest hundredth?
e. Using your equation from part (b) graph $g(x)$ on a graphing calculator. How does $g(x)$ compare to the exponential graph with the same base.

\#65 Calculate each of the values below, then justify your answers by writing the equivalent exponential form.

| a. $\log _{2}(32)=?$ | b. $\log _{2}\left(\frac{1}{2}\right)=?$ |
| :--- | :--- |
| Equivalent Exponential Form: | Equivalent Exponential Form: |
| c. $\log _{2}(4)=?$ | d. $\log _{2}(0)=?$ |
| Equivalent Exponential Form: | Equivalent Exponential Form: |
| Equivalent Exponential Form: |  |

