

5.2.4 How can I transform log functions?

Transformations of Logarithmic Functions



**#85 SOLVE THE LOG MYSTERY!**

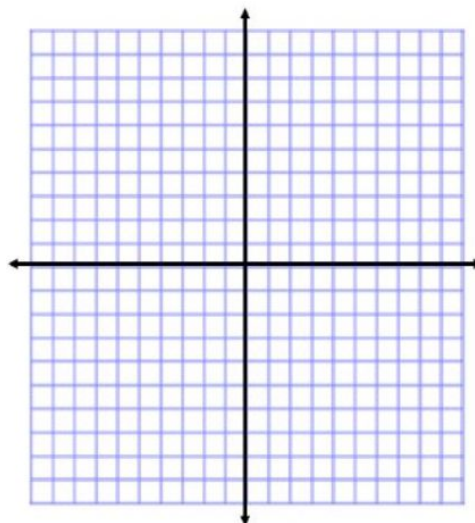
**Your Task:** What is the base of the  $\boxed{\text{LOG}}$  key on your calculator? With your team, start by making a table for  $y = \log(x)$ . Analyze the points in your table, and when you are sure you have figured out the base, write a clear statement justifying your conclusion.

**#86**

a. Complete the following table for  $f(x) = \log(x)$ .

$x$								1	2	3	4	5	6
$f(x)$	-6	-5	-4	-3	-2	-1	0						

b. Make an accurate graph of  $f(x) = \log(x)$ . Remember that just like the graphs of exponential, the graphs of log functions have asymptotes, so make sure any asymptotes on your graph are clearly shown.

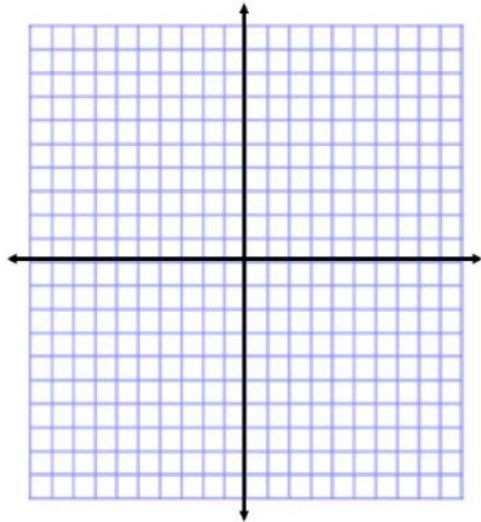


**#87 Continued**

c. What are all of the possible types of transformations of the graph of  $f(x) = \log(x)$ ? For each transformation, show the graph and write its equation.

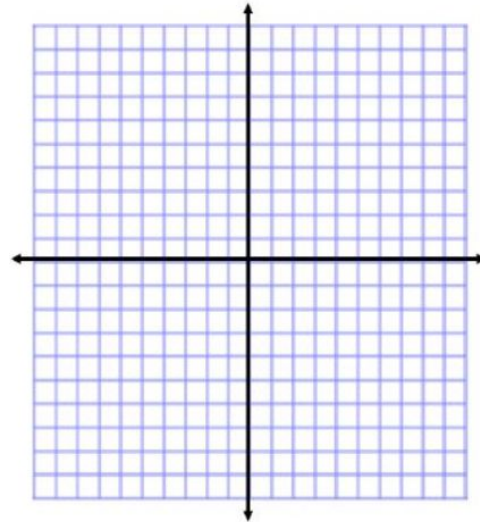
**Shift Left or Right**

Equation:



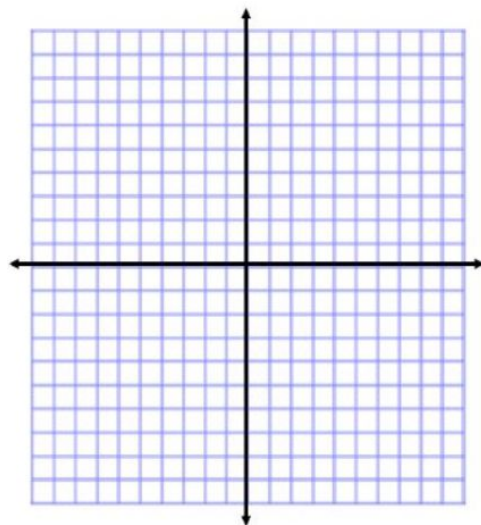
**Shift Up or Down**

Equation:



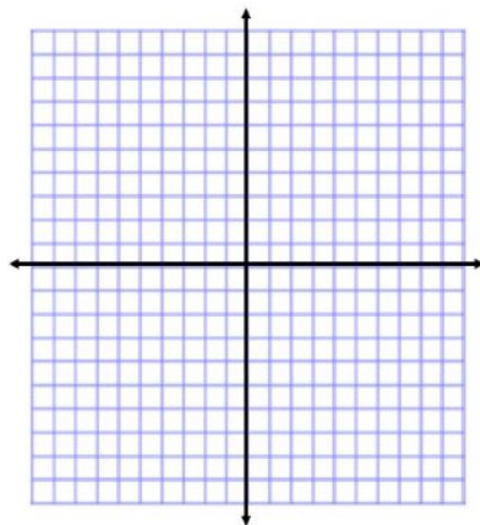
**Reflection across x-axis**

Equation:



**Vertical Stretch or compression**

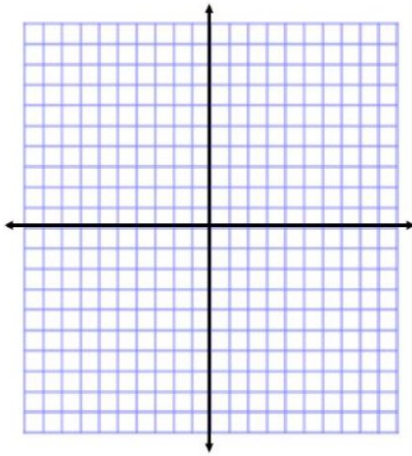
Equation:



Generic Transformation for Family of Logs:

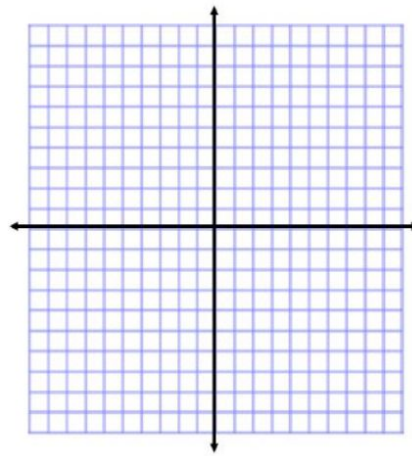
**#87** Sketch a graph of each of the following logarithmic functions without using your graphing calculator. Explain how each graph differs from the parent graph of  $f(x) = \log(x)$ . Once you have completed your work, verify that your graphs are correct using your graphing calculator.

a.  $f_1(x) = \log(x) + 3$



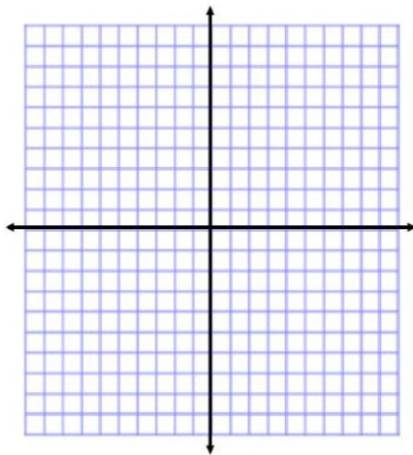
Explain transformation:

b.  $f_2(x) = \log(x - 2)$



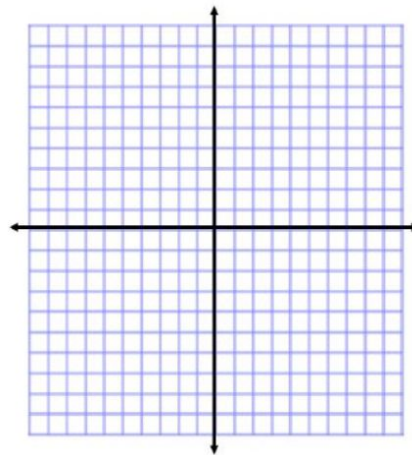
Explain transformation:

c.  $f_3(x) = 4\log(x + 3) - 2$



Explain transformation:

d.  $f_4(x) = \log_2(x) + 3$



Explain transformation: