

CW# _____

Name: _____

7.1.3 How can I write an exponential function?

Writing Equations of Exponential Functions



#31 DUE DATE

Brad's mother has just learned that she is pregnant! Brad is very excited that he will soon become a big brother. Brad's mother says she was tested for HCG during her last two doctor visits. On March 21, her HCG level was 200 mIU/ml (milli-international units per milliliter). Two days later, her HCG level was 392 mIU/ml.

a. Assuming that the model for HCG levels is of the form $y = ab^x$, write an equation that models the growth of HCG for Brad's mother's pregnancy.

i. The doctor visits provide two data points that can help you write an exponential model: (21, 200) and (23, 392). Use each of these points to substitute for x and y into $y = ab^x$. You should end up with two equations in terms of a and b .

ii. Discuss a way to solve your system from part (i) for a and b with your team then solve and write the equation modeling the situation. Be ready to share your method with the class.

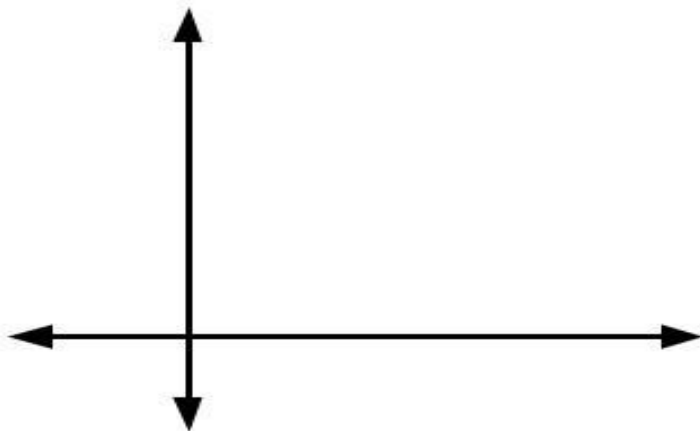
b. Most women maintain an HCG level of 5 mIU/ml before becoming pregnant. Assuming that Brad's mother's level of HCG on the day of implantation was 5 mIU/ml, on what day did the embryo most likely become implanted? How many days after implantation was his mother's first doctor visit?

c. Brad learned that a baby is born approximately 38 weeks after implantation. When can Brad expect his new sibling to be born?

#33 The situation in problem 7-31 required you to assume that the exponential model had an asymptote at $y = 0$ to write the equation of the model. But what if the asymptote is not at the x -axis? Consider the situation below.

a. Assume the graph of an exponential function passes through the points $(3, 12.5)$ and $(4, 11.25)$. Is the exponential function increasing or decreasing? Justify your answer.

b. If the horizontal asymptote for this function is the line $y = 10$, make a sketch of its graph showing the horizontal asymptote.

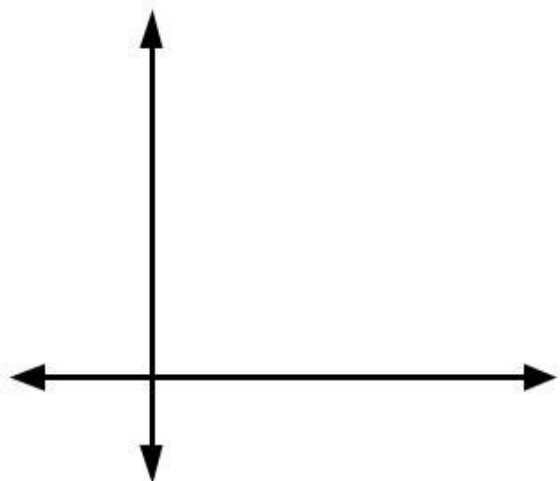


c. If this function has the equation $y = ab^x + k$, what is the value of k ? Use what you know about this function to write its equation. Verify that as x increases, the values of y get closer to $y = 10$.

d. What is the y -intercept of the function? What is the connection between the y -intercept and the asymptote?

Julie has a fresh cup of hot coffee that has a temperature of 180°F . The temperature of the room is 70°F .

a. Sketch a graph of the temperature of the coffee over time.



b. Let t = number of minutes after Julie pours her coffee, and let y = the temperature of the coffee in $^{\circ}\text{F}$. Five minutes after Julie pours her coffee, its temperature is 160°F . Write an equation to model this situation.

c. Julie thinks her coffee is the perfect temperature when it is 130° . When will the coffee be Julie's ideal temperature?

d. What is the temperature of the coffee 10 minutes after it was poured?