

Polynomials**LEARNING PLAN**

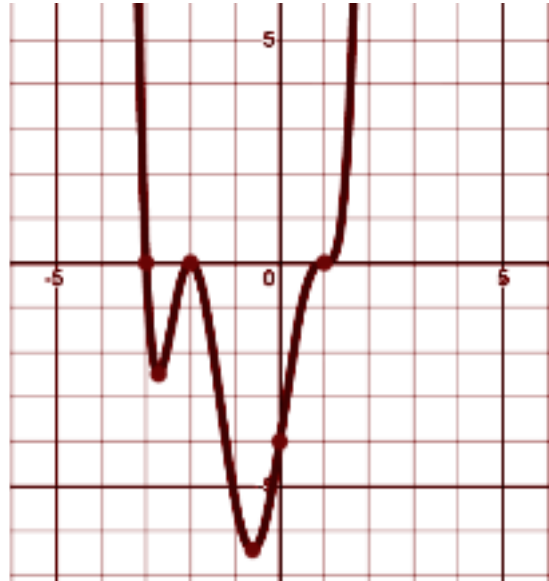
(Chapter 4)

Skill/Understanding:	Review/Practice Problems
<p>Interpreting Equations</p> <ul style="list-style-type: none"> <input type="checkbox"/> Given the equation of a polynomial function in <i>factored form</i>, I can identify the degree, the orientation, the location of x- and y-intercepts, and the shape of the graph at the x-intercepts. <input type="checkbox"/> Given the equation of a polynomial function in <i>standard form</i>, I can identify the degree, the orientation, and the location of the y-intercept. <input type="checkbox"/> I can rewrite the equation of a polynomial function from factored form to standard form, and vice versa. (Using polynomial division or multiplication.) <input type="checkbox"/> I can use polynomial division and the quadratic formula to determine all real and complex roots, or factors, of a polynomial. 	<p>4-42, 4-58, 4-83, 4-122, and CL 4-131.</p>
<p>Writing Equations</p> <ul style="list-style-type: none"> <input type="checkbox"/> Given the graph of a polynomial, I can write a possible equation that accurately represents the orientation, the degree, the location of intercepts, and the shape of the graph at the x-intercepts. <input type="checkbox"/> Given a description of a polynomial curve (intercepts, degree, behavior and an additional point on a graph) I can write the equation of a polynomial function. <input type="checkbox"/> Given the roots (real and complex) of a polynomial, I can write the equation in factored form. 	<p>4-27, 4-76, 4-111, and CL 4-130.</p>
<p>Interpreting Graphs</p> <ul style="list-style-type: none"> <input type="checkbox"/> Given the graph of a polynomial, I can identify the orientation and the minimum degree. <input type="checkbox"/> Given the graph of a polynomial, I can identify the minimum number of real and complex roots. <input type="checkbox"/> Given the graph of a polynomial, I can identify repeated roots (single, double, or triple). 	
<p>Sketching Graphs</p> <ul style="list-style-type: none"> <input type="checkbox"/> I can make a reasonable sketch a polynomial given a description of the graph or an equation. 	<p>4-6, 4-14, 4-44, 4-75, and CL 4-129.</p>

PRACTICE PROBLEMS:

1) The polynomial at right passes through the point $(0, -4)$.

- Find the exact equation of the polynomial with the lowest possible degree.
- What is the degree of the polynomial?
- What are the roots of the polynomial?



2) A 3rd degree polynomial function has roots at $x = -i$ and $x = 2$. The y-intercept is $(0, -6)$. Write an equation for this function in factored form with real coefficients.

3) The roots of a quadratic equation are $x = 2 + i\sqrt{5}$ and $x = 2 - i\sqrt{5}$. Use these to write the equation of the parabola in standard form that has a stretch factor of 1.

4) Make a sketch of the following equation. You do not need to scale but make sure to label the important points:

$$y = -(x + 1)^3(x - 2)^2(x^2 + 6x + 9)$$

5) Give the polynomial $p(x) = x^3 - 3x^2 + x - 3$.

- List all possible factors of $p(x)$.
- List all possible roots of $p(x)$.
- Rewrite $p(x)$ in factored form using polynomial division.
- Which of the possible roots is an actual real root of the polynomial? How can you tell?
- Identify all the roots for $p(x)$.