

Precalculus Honors  
**Exponentials**  
**Toolkit**

Name: \_\_\_\_\_

G

Date: \_\_\_\_\_

Period: \_\_\_\_\_

**Compound Interest**

A = Final Amount

P = Initial Principal Balance

r = Interest Rate

n = Number of times interest is applied per time period

t = number of time periods elapsed

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

Romelle has saved \$4000 and plans to invest it in an account earning 5% interest, compounded quarterly. Assuming no further deposits, how much money will Romelle have in the savings account after  $t$  years?

- I. Why is an exponential model appropriate?

Since we multiply the balance each time by the same number an exponential model is appropriate.

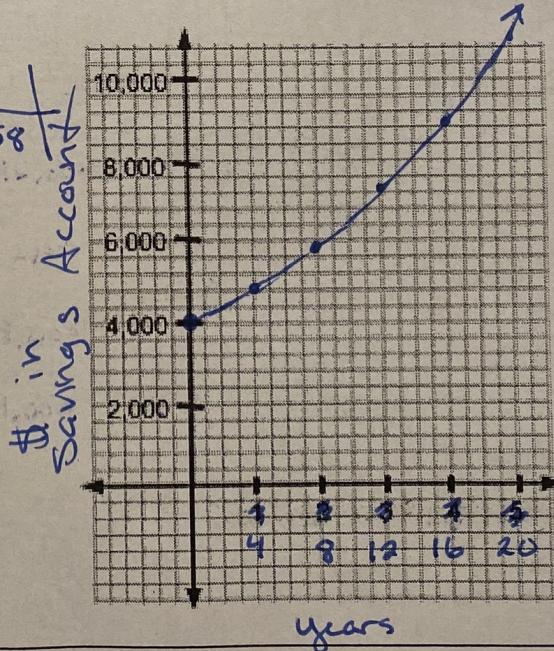
- II. Write an equation that models the situation

$$f(t) = 4000 \left(1 + \frac{0.05}{4}\right)^{4t} \rightarrow f(t) = 4000(1.0125)^{4t}$$

- III. Make a table

Time years	0	4	8	12	16	$t$
\$	4000	4880	5953	7261	8858	
20						10906

- IV. Make a graph



## Standard Exponential Functions

$a$  = Initial Amount

$$y = ab^{(x-h)} + k$$

$b$  = multiplier or constant ratio

$h$  = horizontal shift

$k$  = vertical shift

\* Exponential graphs can be written without the horizontal shift and not all exponential graphs have a vertical shift.

A scientist is growing bacteria, starting with a culture of 5 bacteria. Bacteria "grow" by multiplying. After 2 hours there are 14 bacteria. How many bacteria will be present after  $t$  hours?

- I. Why is an exponential model appropriate?

Since the bacteria is multiplying each time an exponential model is appropriate

- II. Write an equation that models the situation.

$$\begin{aligned} f(t) &= a \cdot b^t \\ f(t) &= 5 \cdot b^t \\ 14 &= 5 \cdot b^2 \end{aligned}$$

$$\begin{aligned} \frac{14}{5} &= b^2 \\ 1.67 &\approx b \end{aligned}$$

$$f(t) = 5(1.67)^t$$

- III. Make a table

x hours	0	2	4	6	8	10
$f(x)$ # of bacteria	5	14	39	108	302	849

- IV. Make a graph

