

### Piecewise Function Notes

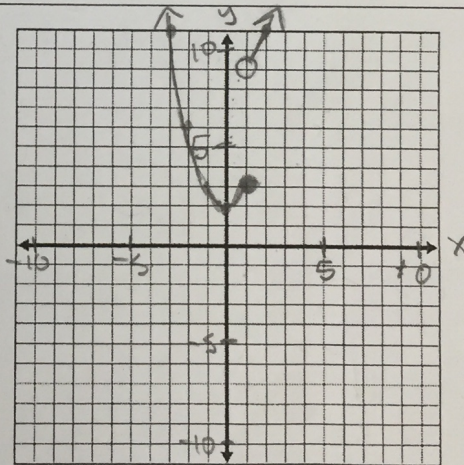
Consider the function  $g(x) = \begin{cases} x^2 + 2 & \text{for } x \leq 1 \\ 2x + 7 & \text{for } x > 1 \end{cases}$

Complete the tables for  $g(x)$  below.

For $x \leq 1$	
$x$	$g(x) = x^2 + 2$
-5	$(-5)^2 + 2 = 27$
-4	$(-4)^2 + 2 = 18$
-3	$(-3)^2 + 2 = 11$
-2	$(-2)^2 + 2 = 6$
-1	$(-1)^2 + 2 = 3$
0	$(0)^2 + 2 = 2$
1	$(1)^2 + 2 = 3$

For $x > 1$	
$x$	$g(x) = 2x + 7$
1	$2(1) + 7 = 9$
2	$2(2) + 7 = 11$
3	$2(3) + 7 = 13$
4	$2(4) + 7 = 15$
5	$2(5) + 7 = 17$
6	$2(6) + 7 = 19$
7	$2(7) + 7 = 21$

Using your table, make a careful sketch of the graph  $y = g(x)$ . Recall the use of open circles to indicate that an endpoint *is not* included and closed circles to indicate that an endpoint *is* included. At which points will the open and closed circles be located on this graph?



What are the domain and the range of this function?

Domain:  $\mathbb{R}$

Range:  $y \geq 2$

Is the piecewise function continuous? Why or why not?

This function is not continuous because you have to pick up your pencil to continue

drawing the graph at  $x = 1$ . We also see if we evaluate  $g(x)$  for each equation you get different values.

### Piecewise Function Notes

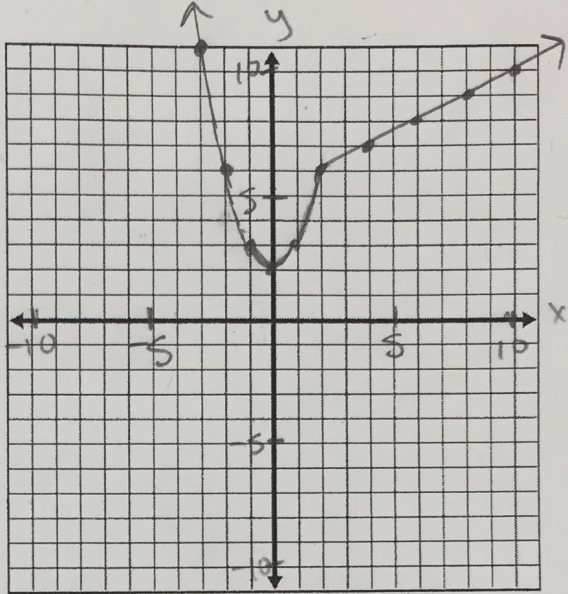
$$\text{Let } f(x) = \begin{cases} x^2 + 2 & \text{for } x \leq 2 \\ \frac{1}{2}x + 5 & \text{for } x > 2 \end{cases}$$

Complete the tables below for  $f(x)$ .

for $x \leq 2$	
x	f(x)
-3	11
-2	6
-1	3
0	2
1	3
2	6

for $x > 2$	
x	f(x)
2	6
4	7
6	8
8	9
10	10

Graph  $f(x)$  below:



State the domain and range of  $f(x)$ .

Domain:  $\mathbb{R}$

Range:  $y \geq 2$

Is the function continuous? Why or why not?

This function is continuous because you do not have to pick up your pencil to completely

Completely describe the function  $f(x)$ .

- No x-intercepts
- y-intercept:  $(0, 2)$
- curved for  $x \leq 2$  (parabola shape)
- linear for  $x > 2$
- Domain & Range stated above
- Decreasing  $x < 0$
- Increasing  $x > 0$
- Function
- Minimum  $y = 2$
- opens up for parabola portion

draw the graph also  
 $f(2) = 6$   
 for both equations and that would be where

the function breaks