

Precalculus Honors  
**Unit Circle Angles**  
**Notes**

Name: \_\_\_\_\_

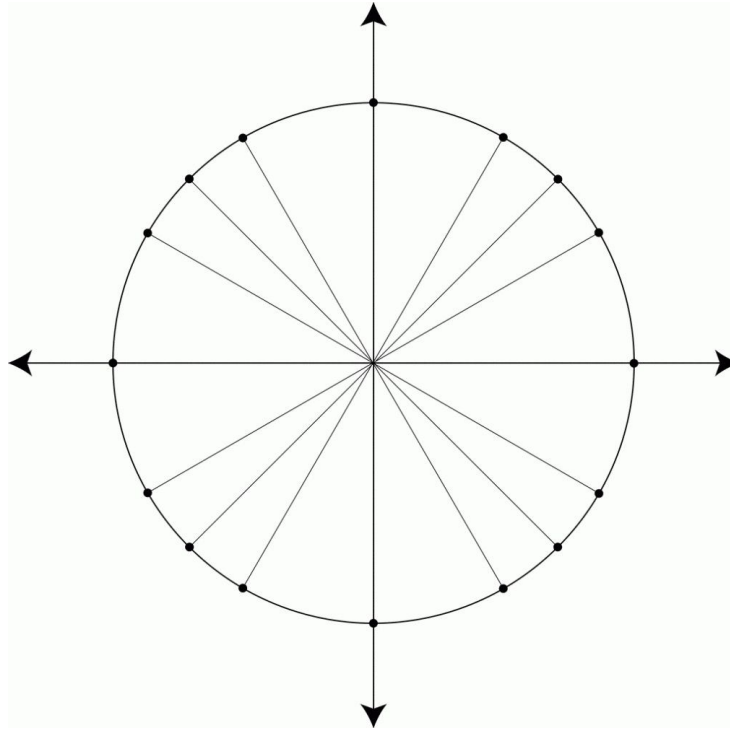
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Use the circle to locate all of the angles with the radian measures listed below.

$0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}, \frac{2\pi}{3}, \frac{3\pi}{4}, \frac{5\pi}{6}, \pi, \frac{7\pi}{6}, \frac{5\pi}{4}, \frac{4\pi}{3}, \frac{3\pi}{2}, \frac{5\pi}{3}, \frac{7\pi}{4}, \frac{11\pi}{6}, 2\pi$



What if you go the other direction? When you move clockwise around the unit circle, starting at the standard position (positive  $x$ -axis), the angle measures are negative. For each part below, what is the positive angle that is **coterminal** (ends up at the same position on the circle) with the given negative angle?

For example,  $-\frac{7\pi}{6}$  is coterminal with  $\frac{5\pi}{6}$ . (Verify this!)

a.  $-\frac{2\pi}{3}$

b.  $-\frac{5\pi}{4}$

c.  $-\frac{11\pi}{6}$

Angle measures can go beyond  $2\pi$  as well. For example,  $\frac{13\pi}{6}$  is coterminal with  $\frac{\pi}{6}$ . For each angle below, state the angle that is coterminal and between 0 and  $2\pi$ .

a.  $\frac{10\pi}{3}$

b.  $\frac{17\pi}{4}$

c.  $-\frac{25\pi}{6}$

Use the angle measures from the previous problem to make some observations about the unit circle. For each part below,  $a$  is an integer.

a. Look at the angles that have measurements of the form  $a\pi$ . Where does the terminal ray of each of these angles intersect the circle?

b. Look at the angles that have measurements of the form  $\frac{a\pi}{2}$ . Where does the terminal ray of each of these angles intersect the circle?

c. Look at the angles that have measurements of the form  $\frac{a\pi}{4}$ . Where does the terminal ray of each of these angles intersect the circle?

d. Look at the angles that have measurements of the form  $\frac{a\pi}{3}$ . Which axis is the terminal ray of each of these angles closest to?

e. Look at the angles that have measurements of the form  $\frac{a\pi}{6}$ . Which axis is the terminal ray of each of these angles closest to?